

Problem 22, Ch. 14, Modern 2.

Note Title

3/28/2008

Grams of ^{235}U to make 1 GW-day?

$$E_p = 1 \text{ GW} \cdot \text{day} = (10^9 \text{ J} \cdot \text{s})(8.64 \times 10^4 \text{ s}) \\ = 8.64 \times 10^{13} \text{ J}$$

1 fission = 200 MeV of energy

$$E_{\text{fission}} = (2 \times 10^8 \text{ eV})(1.6 \times 10^{-19} \text{ J/eV}) \\ = 3.2 \times 10^{-11} \text{ J}$$

$$\text{# fissions} = \frac{E_p}{E_{\text{fission}}} = \frac{8.64 \times 10^{13} \text{ J}}{3.2 \times 10^{-11} \text{ J}} \\ = 2.7 \times 10^{24}$$

This is number of atoms used.

$$\text{Mass used} = (235 \text{ g/mol}) \left(\frac{2.7 \times 10^{24}}{6.02 \times 10^{23}} \right) \\ = 1053 \text{ g} \approx 1 \text{ kg}$$

By contrast, Coal has a chemical energy density of about 25 MJ/kg

$$\text{So this would take } \frac{8.64 \times 10^{13} \text{ J}}{2.5 \times 10^7 \text{ J/kg}} \\ = 3.5 \times 10^6 \text{ kg} = 3500 \text{ tonnes of coal.}$$